

Lecture 11: Pointer Analysis

17-355/17-655/17-819: Program Analysis

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March 11, 2021

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Extending WHILE3ADDR with Pointers

$I ::= \dots$	
$p := \&x$	taking the address of a variable
$p := q$	copying a pointer from one variable to another
$*p := q$	assigning through a pointer
$p := *q$	dereferencing a pointer

Consider Constant Propagation

```
1 : z := 1  
2 : p := &z  
3 : *p := 2  
4 : print z
```

Need to know that line 3 changes variable z!

Consider Constant Propagation

1 : $z := 1$

2 : **if** (*cond*) $p := \&y$ **else** $p := \&z$

3 : $*p := 2$

4 : **print** z

Points-To Analysis: May vs. Must and Strong Updates

$$f_{CP}[*p := y](\sigma) = \sigma[z \mapsto \sigma(y) \mid z \in \text{must-point-to}(p)]$$

$$f_{CP}[*p := y](\sigma) = \sigma[z \mapsto \sigma(z) \sqcup \sigma(y) \mid z \in \text{may-point-to}(p)]$$

Pointer Analysis

- Two common relations used as abstract values
 - Alias analysis: (x, y) alias pairs
 - Points-to analysis: $p \rightarrow q$ // or sets for points-to(p)
 - Both have *may* and *must* versions
- Very expensive to run precisely as data-flow analysis
 - Lattice is $2^{\text{Var} \times \text{Var}}$. Yikes!
 - Almost always needs to be inter-procedural
 - (even if used for intra-procedural optimizations)
 - Context-sensitivity is often important for adequate precision

Andersen's Analysis

- Flow-insensitive analysis
 - Considers only *nodes* of a CFG (i.e., instructions) and ignores all edges
 - What? Yes, really.
 - Trades-off precision for tractability
 - Can be combined with *context-sensitive* techniques
- Key idea: cast as constraint-solving problem
 - Abstract model of memory locations and points-to sets
 - Let l_x represent location of var x
 - Let p be the set of locations pointed-to by var p
 - One subset constraint per instruction
 - Invoke constraint solver. Done!

Andersen's Analysis

$$\frac{}{\llbracket p := \&x \rrbracket \hookrightarrow l_x \in p} \text{address-of}$$

$$\frac{}{\llbracket p := q \rrbracket \hookrightarrow p \supseteq q} \text{copy}$$

$$\frac{}{\llbracket *p := q \rrbracket \hookrightarrow *p \supseteq q} \text{assign}$$

$$\frac{}{\llbracket p := *q \rrbracket \hookrightarrow p \supseteq *q} \text{dereference}$$

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$$\frac{p \supseteq q \quad l_x \in q}{l_x \in p} \text{copy}$$

$$\frac{*p \supseteq q \quad l_r \in p \quad l_x \in q}{l_x \in r} \text{assign}$$

$$\frac{p \supseteq *q \quad l_r \in q \quad l_x \in r}{l_x \in p} \text{dereference}$$

Example

```
x := 42
y := 108
q := &x
if (..)
    p := q
else
    p := &y
r = &p
s = *r
print(*s)
print(*q)
```

$$\overline{[\![p := \&x]\!]} \hookrightarrow l_x \in p \quad \textit{address-of}$$

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$$\overline{[\![*p := q]\!]} \hookrightarrow *p \supseteq q \quad \textit{assign}$$

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Dynamic Memory Allocation?

```
1 : q := malloc()  
2 : p := malloc()  
3 : p := q  
4 : r := &p  
5 : s := malloc()  
6 : *r := s  
7 : t := &s  
8 : u := *t
```

Dynamic Memory Allocation

```
1 : q := malloc()  
2 : p := malloc()  
3 : p := q  
4 : r := &p  
5 : s := malloc()  
6 : *r := s  
7 : t := &s  
8 : u := *t
```

$$\overline{[\![n: p := \text{malloc}()]\!]} \hookrightarrow l_n \in p \quad \text{malloc}$$

Exercise

- 1 : $q := \text{malloc}()$
- 2 : $p := \text{malloc}()$
- 3 : $p := q$
- 4 : $r := \&p$
- 5 : $s := \text{malloc}()$
- 6 : $*r := s$
- 7 : $t := \&s$
- 8 : $u := *t$

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$$\frac{}{\llbracket n: p := \text{malloc}() \rrbracket \hookrightarrow l_n \in p} \text{malloc}$$

Efficiency

- $O(n)$ constraints
- $O(n)$ firings per copy-constraint
- $O(n^2)$ firings per assign/deref-constraint
- Worst-case $O(n^3)$ firings
- Can be solved in $O(n^3)$ time
 - McAllester [SAS'99]
- $O(n^2)$ in practice
 - Sridharan et al. [SAS'09]
 - K -sparseness property

$$\frac{}{\llbracket p := \&x \rrbracket \hookrightarrow l_x \in p} \text{address-of}$$

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Field-Sensitivity

1 : $p.f := \&x$

2 : $p.g := \&y$

Field-Sensitivity

1 : $p.f := \&x$

2 : $p.g := \&y$

A field-insensitive approach just treats fields `. f ' as dereferences `*`.

Field-Sensitive Analysis

$$\frac{}{\llbracket p := q.f \rrbracket \hookrightarrow p \supseteq q.f} \textit{field-read}$$

$$\frac{}{\llbracket p.f := q \rrbracket \hookrightarrow p.f \supseteq q} \textit{field-assign}$$

Field-Sensitive Analysis

$$\frac{}{\llbracket p := q.f \rrbracket \hookrightarrow p \supseteq q.f} \text{field-read}$$

$$\frac{}{\llbracket p.f := q \rrbracket \hookrightarrow p.f \supseteq q} \text{field-assign}$$

$$\frac{p \supseteq q.f \quad l_q \in q \quad l_f \in l_{q.f}}{l_f \in p} \text{field-read}$$

$$\frac{p.f \supseteq q \quad l_p \in p \quad l_q \in q}{l_q \in l_{p.f}} \text{field-assign}$$

Field-Sensitive Analysis

$$\frac{}{\llbracket p := q.f \rrbracket \hookrightarrow p \supseteq q.f} \text{field-read}$$

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$$\frac{p.f \supseteq q \quad l_p \in p \quad l_q \in q}{l_q \in l_{p.f}} \text{field-assign}$$

```
a := new X()
b := new Y()
c := new Y()
a.f := b
a.g := c
print(a.f)
```

Steengaard's Analysis

- **Problem:** Quadratic-in-practice is still not ultra-scalable
- **Challenge:** Need ~LINEAR. How?
 - Solution space of pointer analysis (e.g. points-to sets) itself is $O(n^2)$.
- **Key idea:** Use constant-space per pointer. Merge aliases and alternates into the same equivalence class.
 - p can point to q or r ? Let's treat q and r as the same pseudo-var and merge everything we know about q and r .
 - Points-to “sets” are basically singletons

Steensgaard's Analysis - Example

1 : $p := \&x$

2 : $r := \&p$

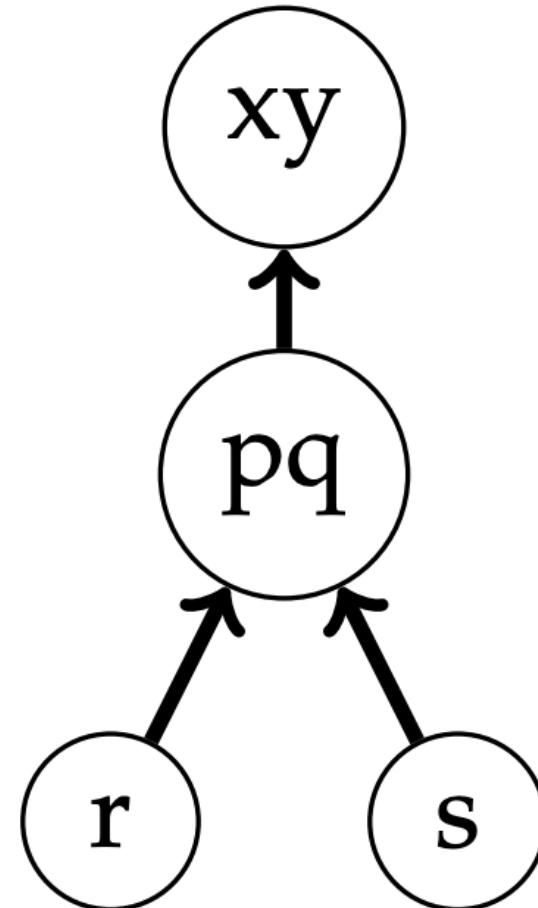
3 : $q := \&y$

4 : $s := \&q$

5 : $r := s$

Steengaard's Analysis - Example

```
1 : p := &x  
2 : r := &p  
3 : q := &y  
4 : s := &q  
5 : r := s
```



Steensgaard's Analysis - Exercise

```
1 :  a := &x
2 :  b := &y
3 :  if p then
4 :      y := &z
5 :  else
6 :      y := &x
7 :  c := &y
```

Steengaard's Analysis

$$\frac{}{\llbracket p := q \rrbracket \hookrightarrow \text{join}(*p, *q)} \text{copy}$$

$$\frac{}{\llbracket p := \&x \rrbracket \hookrightarrow \text{join}(*p, x)} \text{address-of}$$

$$\frac{}{\llbracket p := *q \rrbracket \hookrightarrow \text{join}(*p, **q)} \text{dereference}$$

$$\frac{}{\llbracket *p := q \rrbracket \hookrightarrow \text{join}(**p, *q)} \text{assign}$$

Steengaard's Analysis

	join(ℓ_1, ℓ_2)
$\boxed{[p := q]} \hookrightarrow \text{join}(*p, *q)$	copy <pre>if (find(ℓ_1) == find(ℓ_2)) return</pre>
$\boxed{[p := &x]} \hookrightarrow \text{join}(*p, x)$	address-of $n_1 \leftarrow * \ell_1$ $n_2 \leftarrow * \ell_2$ union(ℓ_1, ℓ_2)
$\boxed{[p := *q]} \hookrightarrow \text{join}(*p, **q)$	dereference join(n_1, n_2)
$\boxed{[*p := q]} \hookrightarrow \text{join}(**p, *q)$	assign

Steengaard's Analysis

- Abstract locations implemented as *union-find* data structure
 - Each union and find operation takes $O(\alpha(n))$ time each
 - Total algorithm running time is $O(n * \alpha(n)) \sim$ almost linear
 - Space consumption is linear
- In practice: very scalable
 - Millions of LoC

OOP: Dynamic Dispatch

```
class A { A foo(A x) { return x; } }
class B extends A { A foo(A x) { return new D(); } }
class D extends A { A foo(A x) { return new A(); } }
class C extends A { A foo(A x) { return this; } }

// in main()
A x = new A();
while (...) {
    x = x.foo(new B()); // may call A.foo, B.foo, or D.foo
A y = new C();
y.foo(x);           // only calls C.foo
```